

Examen de Matemáticas 4º de ESO

Noviembre 2009

Resolver las siguientes ecuaciones y sistemas:

Problema 1

$$\log(2x + 3) - 2 \log x = 2$$

Solución:

$$\log\left(\frac{2x + 3}{x^2}\right) = \log 100 \implies 100x^2 - 2x - 3 = 0 \implies$$

$$\begin{cases} x = 0,1834935157 \\ x = -0,1634935157 \text{ No Vale} \end{cases}$$

Problema 2

$$5^{2x-1} + 5^{x+1} - 1 = 0$$

Solución:

$$\frac{(5^x)^2}{5} + 5 \cdot 5^x - 1 = 0 \implies \frac{t^2}{5} + 5t - 1 = 0 \implies \begin{cases} t = 0,1984250992 \\ t = -25,19842509 \end{cases}$$

$$\begin{cases} t = 0,1984250992 = 5^x \implies x = -1,004912070 \\ t = -25,19842509 = 5^x \implies \text{No Vale} \end{cases}$$

Problema 3

$$\begin{cases} \log(xy^2) = 8 \\ \log\left(\frac{x^2}{y}\right) = 1 \end{cases}$$

Solución:

$$\begin{cases} \log x + 2 \log y = 8 \\ 2 \log x - \log y = 1 \end{cases} \implies \begin{cases} u + 2v = 8 \\ 2u - v = 1 \end{cases} \implies$$

$$\begin{cases} u = \log x = 2 \implies x = 100 \\ v = \log y = 3 \implies y = 1000 \end{cases}$$

Problema 4

$$\begin{cases} 2^{x-1} + 3^{y+1} = 10 \\ 2^x - 3^y = 6 \end{cases}$$

Solución:

$$\begin{cases} \frac{2^x}{2} + 3 \cdot 3^y = 10 \\ 2^x - 3^y = 3 \end{cases} \implies \begin{cases} \frac{u}{2} + 3v = 10 \\ u - v = 6 \end{cases} \implies \begin{cases} u = 8 = 2^x \implies x = 3 \\ v = 2 = 3^y \implies y = 0,6309297535 \end{cases}$$

Problema 5

$$\frac{x-2}{2} - \frac{x-1}{7} \geq 1 - \frac{x+1}{14}$$

Solución:

$$5x - 12 \geq 13 - x \implies x \geq \frac{25}{6} \implies \left[\frac{25}{6}, \infty \right)$$

Problema 6

$$\frac{x^2 + 4x - 5}{x + 2} \geq 0$$

Solución:

$$\frac{x^2 + 4x - 5}{x + 2} = \frac{(x-1)(x+5)}{x+2} \geq 0$$

	$(-\infty, -5)$	$(-5, -2)$	$(-2, 1)$	$(1, \infty)$
$f(x)$	$-$	$+$	$-$	$+$

La solución es: $[-5, -2) \cup [1, \infty)$

Problema 7

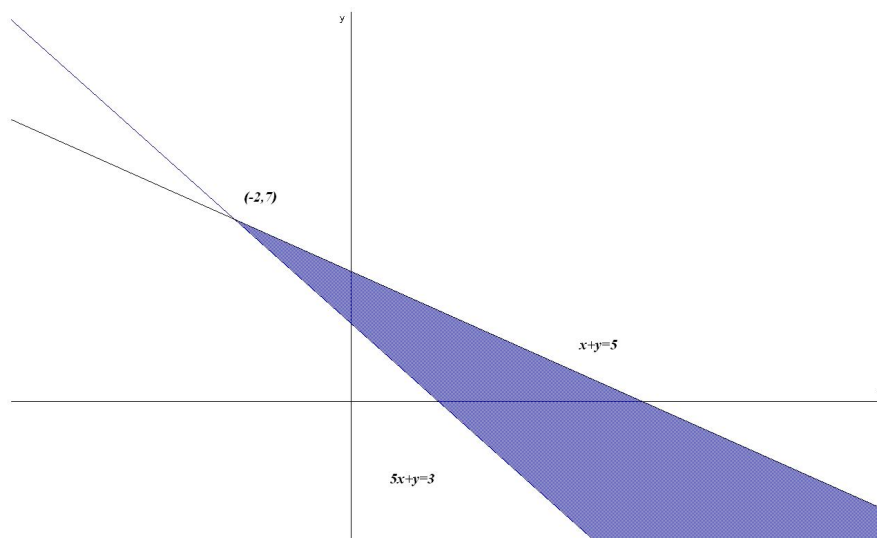
$$\begin{cases} x + y \leq 5 \\ 2x + y \geq 3 \end{cases}$$

Solución:

$$x + y = 5 \implies \begin{array}{c|c} x & y \\ \hline 0 & 5 \\ 5 & 0 \end{array}$$

$$2x + y = 3 \implies \begin{array}{c|c} x & y \\ \hline 0 & 3 \\ 3/2 & 0 \end{array}$$

$$\begin{cases} x + y = 5 \\ 2x + y = 3 \end{cases} \implies \begin{cases} x = -2 \\ y = 7 \end{cases} \implies (-2, 7)$$



Problema 8

$$\sqrt{2x+5} - \sqrt{x-1} = 2$$

Solución:

$$\begin{aligned} (\sqrt{2x+5})^2 &= (2 + \sqrt{x-1})^2 \implies 2x+5 = 4 + x-1 + 4\sqrt{x-1} \\ \implies x^2 - 12x + 20 &= 0 \implies x = 2, \text{ y } x = 10 \end{aligned}$$

Problema 9

$$3 - \sqrt{x-1} = x$$

Solución:

$$\begin{aligned} -\sqrt{x-1} &= x-3 \implies x-1 = x^2 + 9 - 6x \implies x^2 - 7x + 10 = 0 \implies \\ &\left\{ \begin{array}{l} x = 2 \\ x = 5 \text{ No Vale} \end{array} \right. \end{aligned}$$

Problema 10

$$x^4 + x^2 - 2 = 0$$

Solución:

$$\text{Hacemos } z = x^2 \implies z^2 + z - 2 = 0 \implies z = 1 \text{ y } z = -2.$$

$$z = 1 = x^2 \implies x = \pm 1$$

$$z = -2 = x^2 \text{ No Vale}$$